

Shell-model progress in the investigation of ^{132}Sn mass region

Houda NAÏDJA

In Collaboration with **Frédéric NOWACKI**

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20th Colloque GANIL 2017

Amboise October 15-20, 2017

Introduction

G. S. Simpson et al., PRL 113, 132502 (2014)

H. Naïdja et al., J. Phys. Conf. Series 580, 012030 (2015)

H. Naïdja et al., Acta. Phys. Pol B 46, 669 (2015)

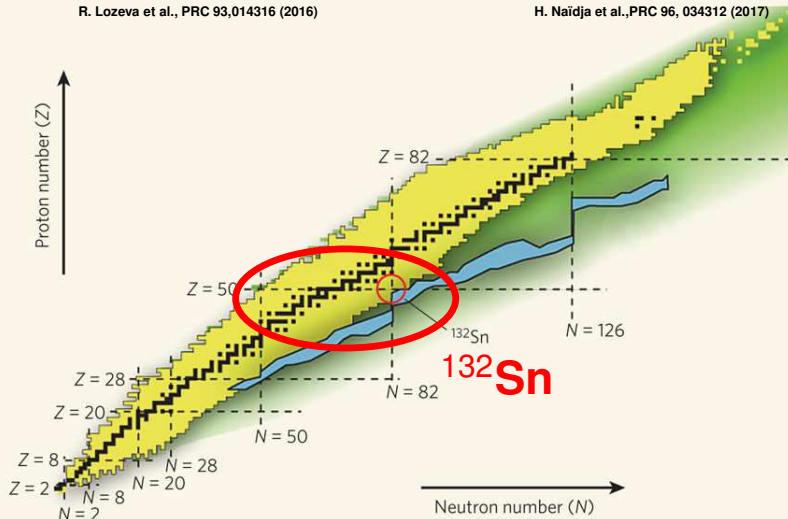
R. Lozeva et al., PRC 93,014316 (2016)

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Low-lying state energies and isomeric transitions in $^{134,136,138}\text{Sn}$

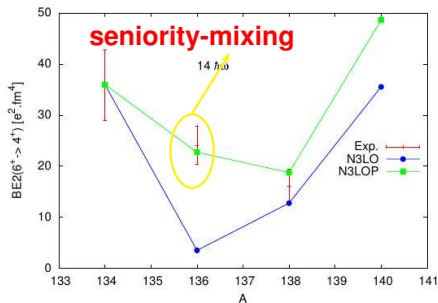
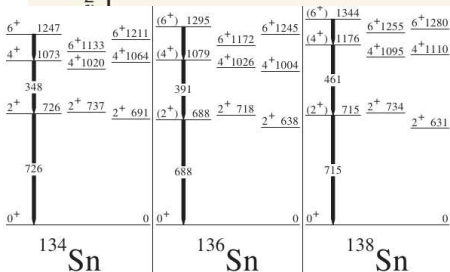
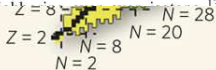


FIG. 4. Proposed level schemes of ^{136}Sn and ^{138}Sn , along with



Neutron number (N)

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H. Naidja et al., PRC 96, 034312 (2017)

Non sub-shell closure at N=90, and the tins masses

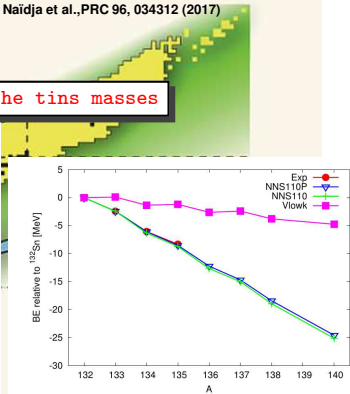
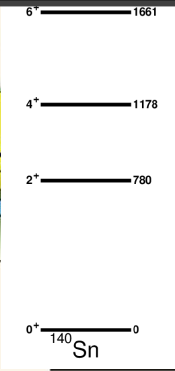
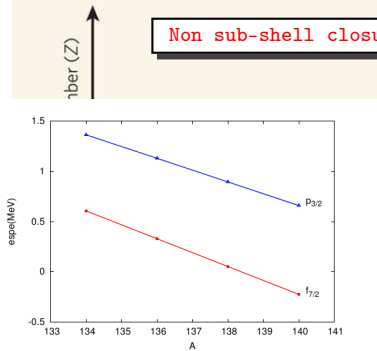
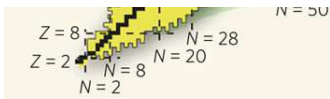


Fig. 3. Binding energies of tin isotopes relative to ^{132}Sn .



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Revised level scheme of ^{136}Sb , and the first spectroscopic information on ^{140}Sb

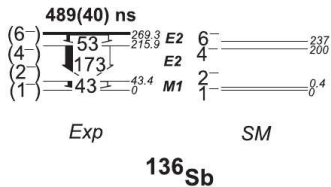


FIG. 2. Revised experimental level scheme of the 6^- isomer in ^{136}Sb compared to shell-model (SM) calculations.

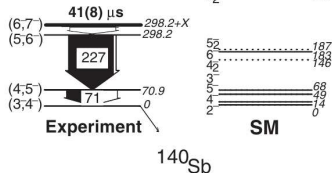
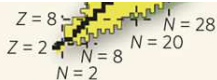


FIG. 2. Experimental level scheme of the observed isomer in ^{140}Sb compared to the results of SM calculations. Yrast and yrare states are represented by solid and dotted lines, respectively.



Neutron number (N)

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High spin states and collectivity in ^{142}Ba and ^{144}Ce

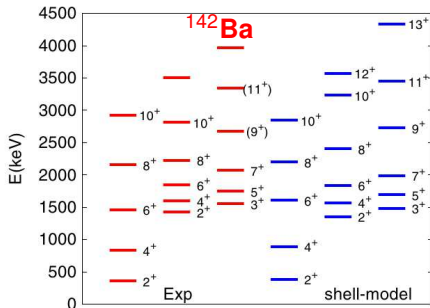


FIG. 9. Excited levels in ^{142}Ba calculated using the N3LOF effective interaction (blue lines), compared to the experimental scheme (red lines).

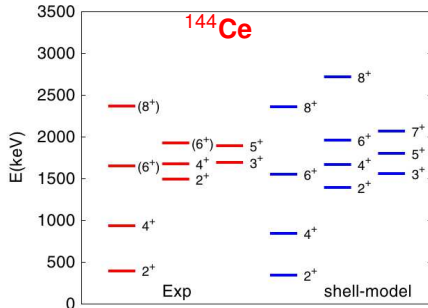


FIG. 10. Excited levels in ^{144}Ce calculated using the N3LOP effective interaction (blue lines), compared to the experimental scheme (red lines).

$N = 2$

Neutron number (N)

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H. Naïdja et al., PRC 95, 064303 (2017)
✉ H. Naïdja et al., PRC 96, 034312 (2017)

spectroscopy and collectivity in Xe, Te, Ba, Ce, Nd nuclei, $N=82,84,86$

umber

$Z = 82$

PHYSICAL REVIEW C **96**, 034312 (2017)

Shell-model investigation of spectroscopic properties and collectivity in the nuclei beyond ^{132}Sn

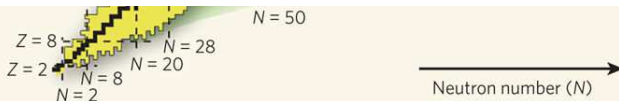
H. Naïdja,^{1,2,3} F. Nowacki,¹ and B. Bounthong¹

¹Université de Strasbourg, CNRS, IPHC UMR 7178, F-67000 Strasbourg, France

²GSI Helmholtzzentrum für Schwerionenforschung GmbH, 64291 Darmstadt, Germany

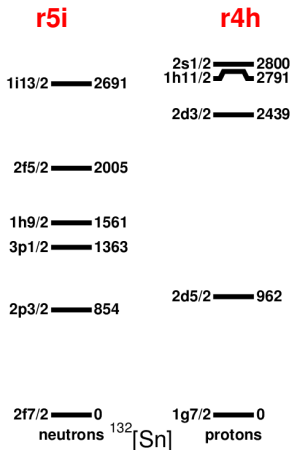
³Université Constantine 1, LPMS, route Ain El Bey 25000 Constantine, Algeria

(Received 20 June 2017; published 13 September 2017)



Shell-model overview

Model space



Diagonalization with **Antoine** and **Nathan**
Strasbourg SM codes.

Effective interaction

- 1 derived from realistic interaction
N3LO
- 2 renormalised by V_{low-k} to exclude the repulsive short range (cutoff $\Lambda = 2.2\text{fm}^{-1}$).
- 3 adapted to the model space by many body perturbation theory,

$$V_{eff} = \underbrace{V_{low} + V_{low} \frac{Q}{E - H_0} V_{low}}_{\text{second order}} + V_{low} \frac{Q}{E - H_0} V_{low} \frac{Q}{E - H_0} V_{low} \frac{Q}{E - H_0} V_{low}$$

- 4 Monopole and Multipole adjustments to N3LO interaction

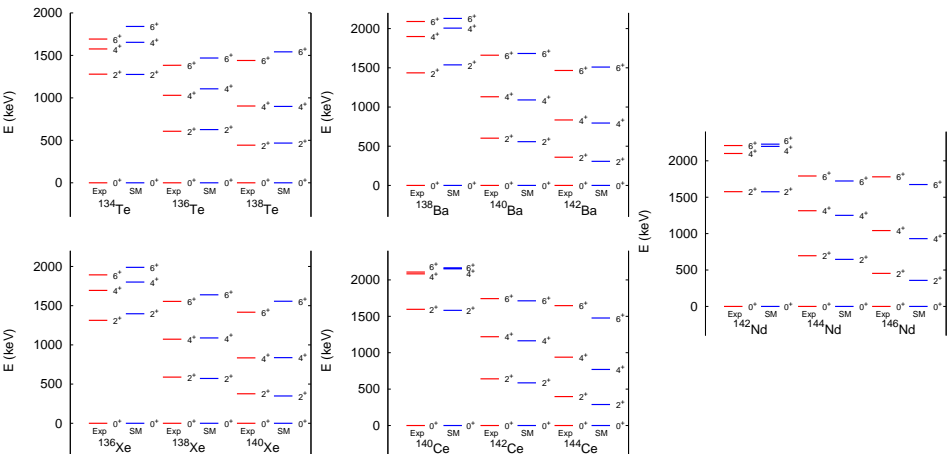
↓
N3LOP interaction

Part I : Spectroscopy and collectivity in even-even nuclei

Te, Xe, Ba, Ce, Nd with $82 \leq N \leq 88$

Energy levels of Te, Xe, Ba, Ce, Nd $82 \leq N \leq 86$

H. Naïdja, F. Nowacki and B. Bounthong, PRC 96, 034312 (2017).



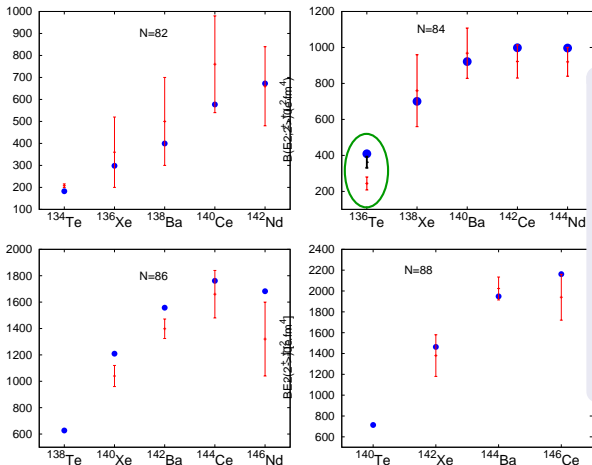
A compression in the level schemes from $N=82$ to $N=86$ isotones



sign of collectivity

E2 Transitions

H. Naïdja, F. Nowacki and B. Bounthong, PRC 96, 034312 (2017).



- ✓ The overestimated ^{136}Te strength is now consistent with the new measurement

J. M. Allmond *et al.* PRL. 118, 092503 (2017)

- ✓ small $B(E2)$ in N=82 isotones due to spherical character
- ✓ strong $B(E2)$ in N=86 and 88 isotones, reflecting the presence of collective character

$$(e_{\text{eff}}(\nu), e_{\text{eff}}(\pi)) = (0.6e, 1.6e)$$

M1 Moments

H. Naidja, F. Nowacki and B. Bounthong, PRC 96, 034312 (2017).

FREE g -FACTORS

$$(g_{\pi}^S, g_{\pi}^I) = (5.5857, 1.0)$$

$$(g_{\nu}^S, g_{\nu}^I) = (-3.8263, 0.0)$$

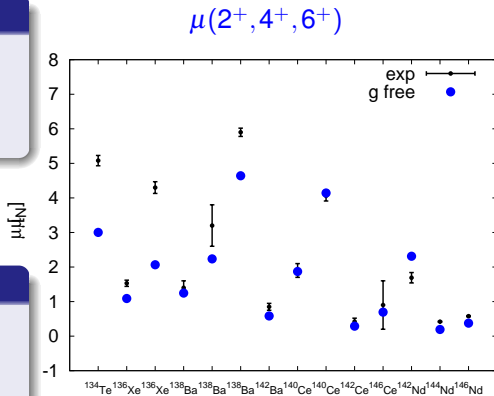
☞ overall bad agreement with the data

EFFECTIVE g -FACTORS

$$(g_{\pi}^S, g_{\pi}^I) = (3.250, 1.069)$$

$$(g_{\nu}^S, g_{\nu}^I) = (-1.506, 0.019)$$

☞ overall good agreement with the data



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H. Naidja, F. Nowacki and B. Bounthong, PRC 96, 034312 (2017).

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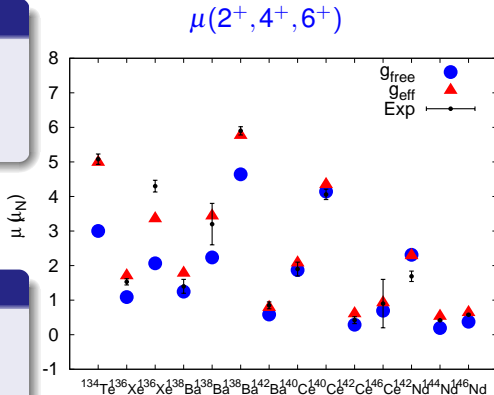
🔴 overall bad agreement with the data

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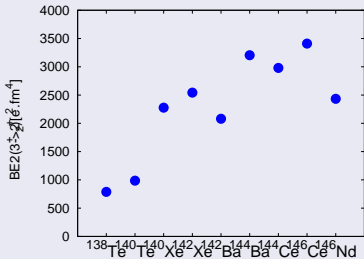
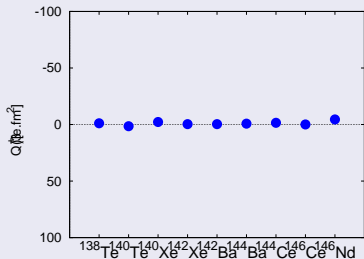
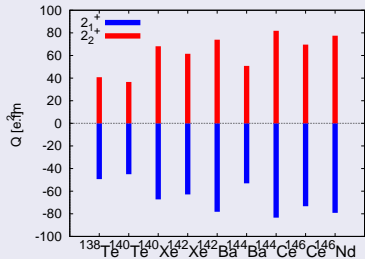
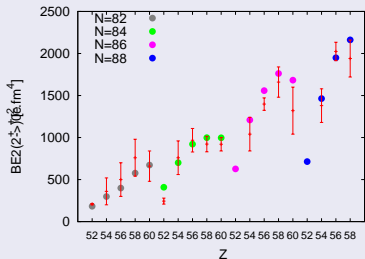
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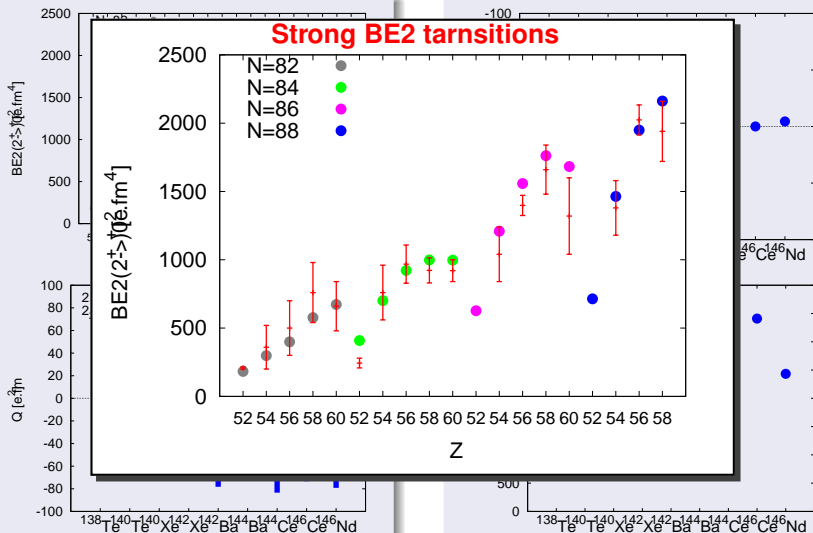
Signs of Collectivity in N=86, 88 isotones

H. Naïdja, F. Nowacki and B. Bounthong, PRC 96, 034312 (2017).



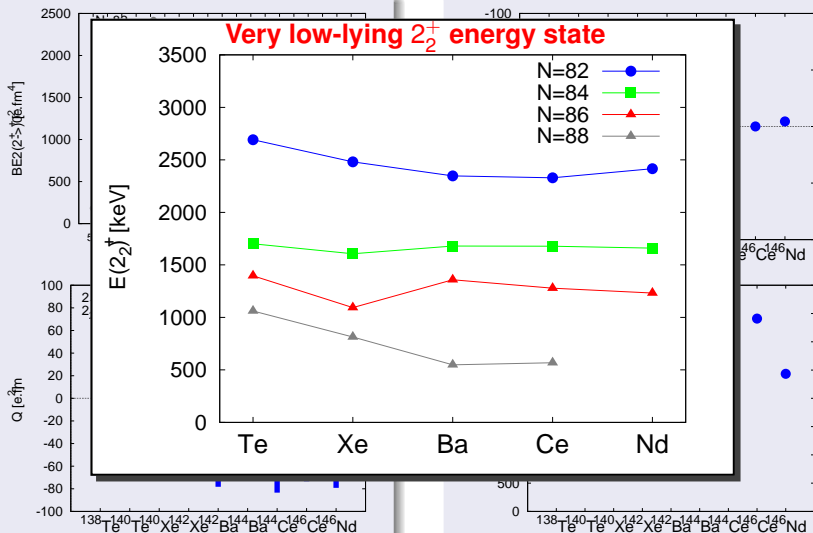
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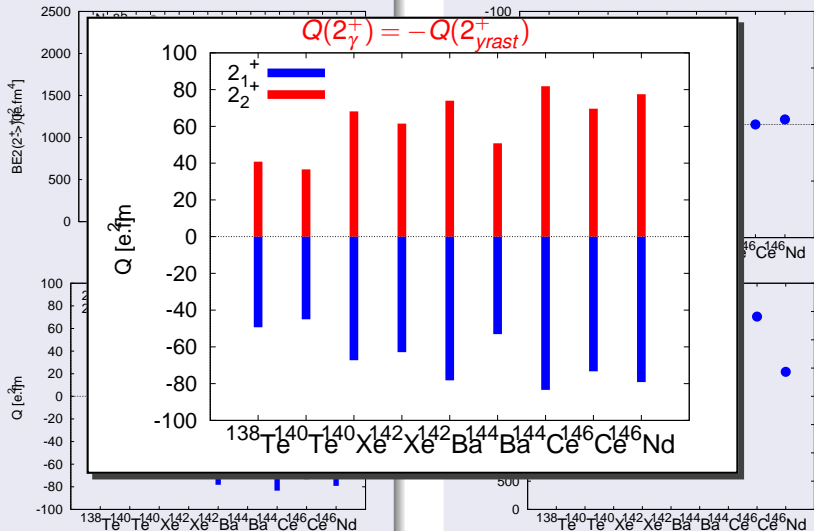
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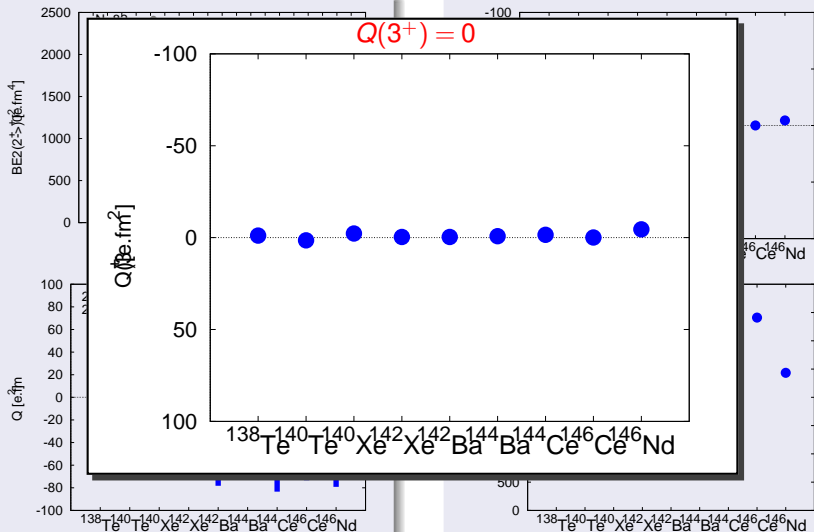
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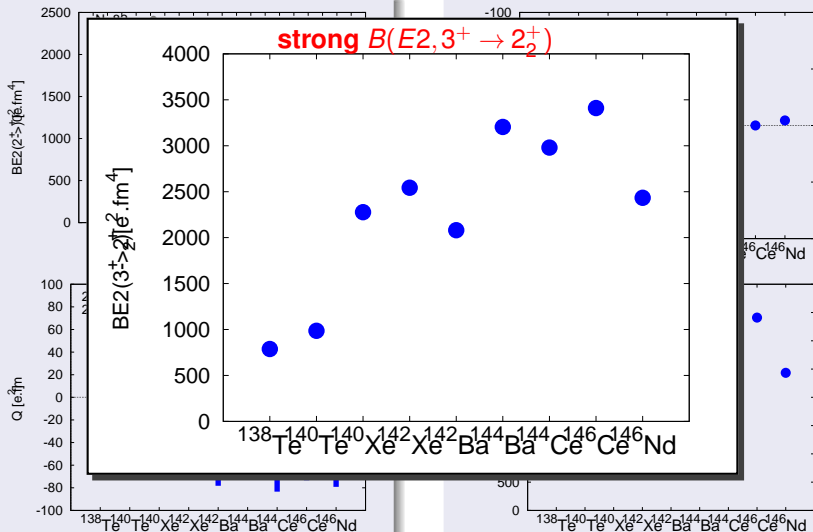
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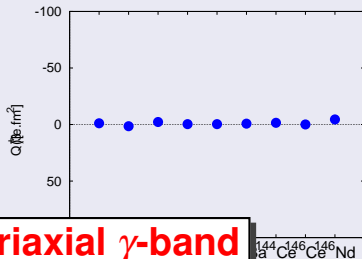
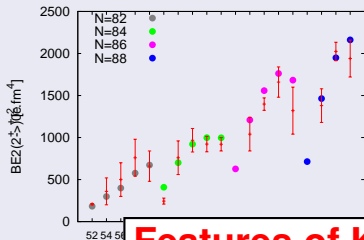
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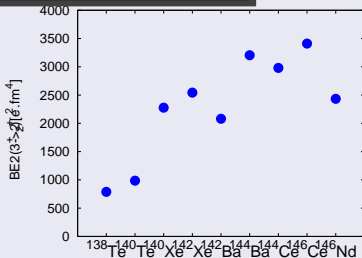
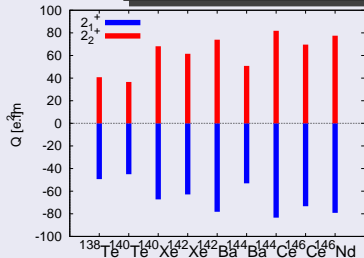


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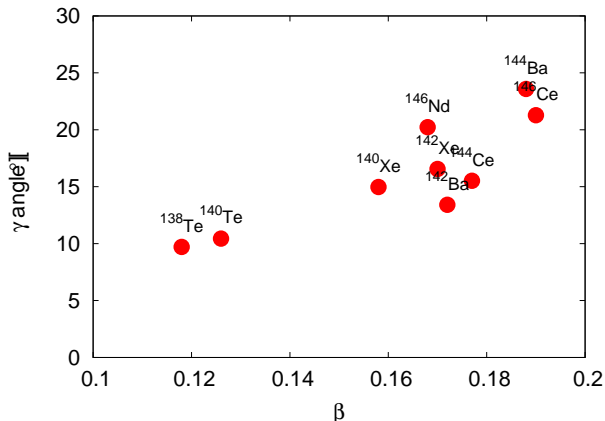


Features of K=2 triaxial γ -band



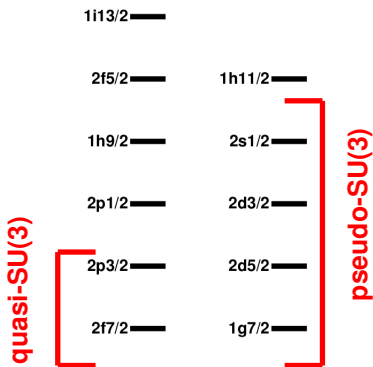
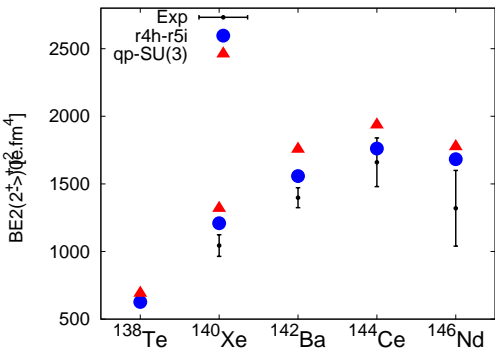
Deformation parameters

β deformation parameter and γ angle*



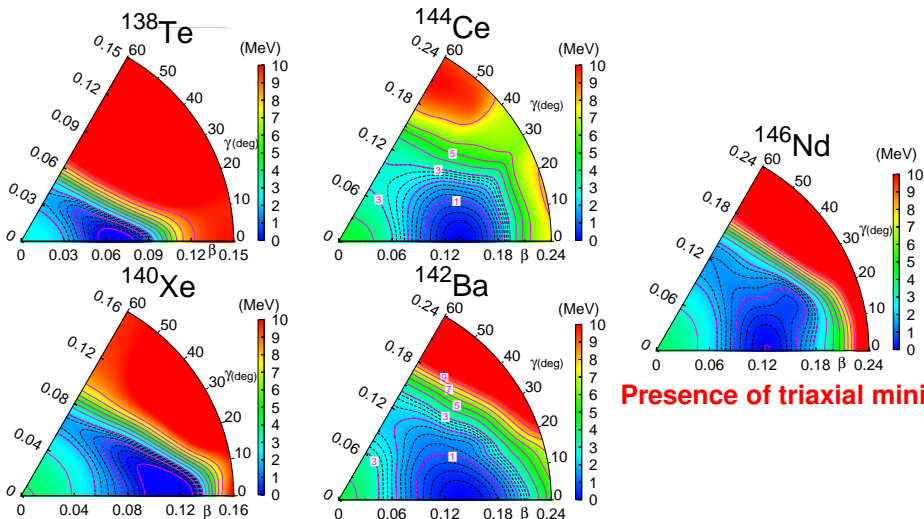
- Mild deformation in ^{138}Te and ^{140}Te .
- Increase in deformation with non-axiality from ^{140}Xe to ^{146}Nd .
- The maximum of the collectivity in ^{144}Ba and ^{146}Ce

SU(3) symmetries vs collectivity



- minor impact of pseudo-SU(3) / quasi-SU(3)
- Excitations to $\pi h_{11/2}$ reduce the collectivity due to the pairing effect, which confirms our previous conclusion in ^{140}Sm analysis with ^{100}Sn core
[M.Klintefjord, et al, PRC 93, 054303 \(2016\)](#)

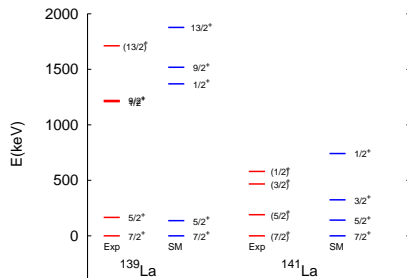
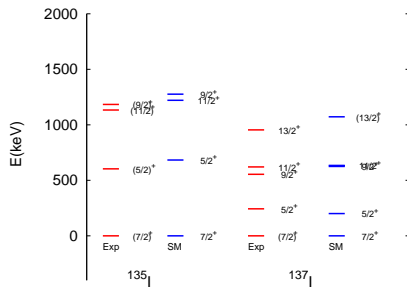
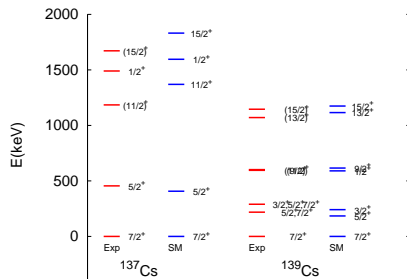
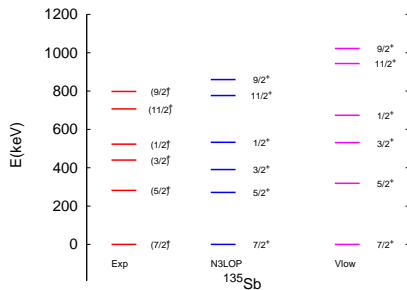
PES with CHFSM



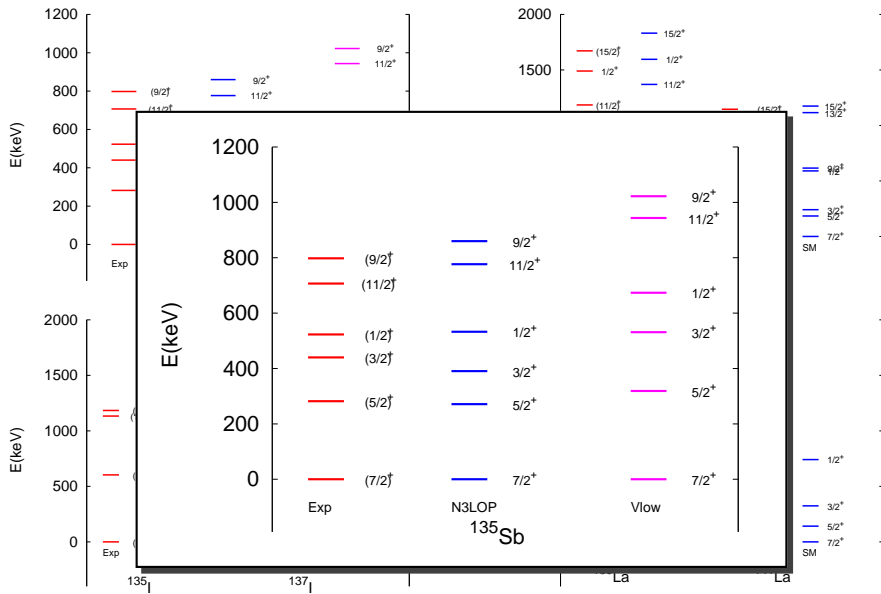
- CHFSM is an approach developed by Strasbourg SM group :
B. Bounthong, PhD Thesis, Université de Strasbourg (2016)
- The same SM Hamiltonian (N3LOP) and the same model space (r4h-r5i) are used
- (β, γ) are consistent with Kumar

Part II : Even-odd and odd-even nuclei

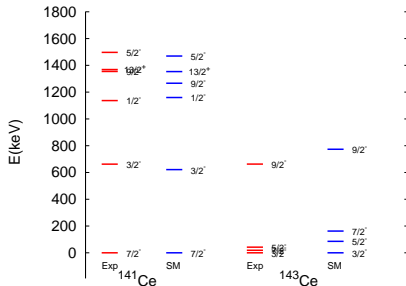
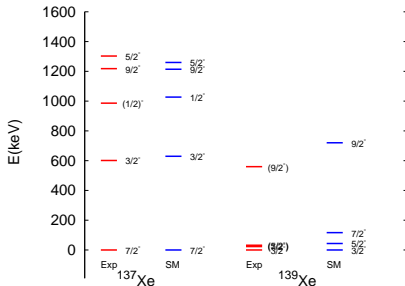
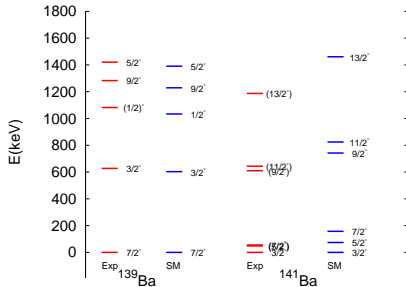
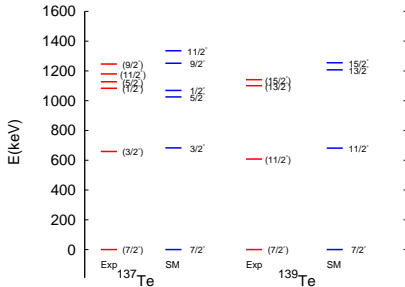
odd-even nuclei : Sb, I, Cs, La



odd-even nuclei : Sb, I, Cs, La

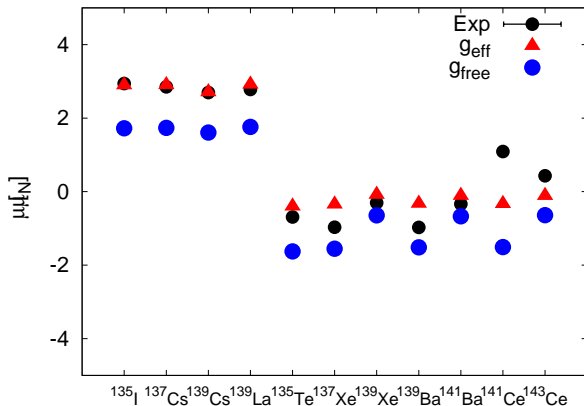


even-odd nuclei : Te, Xe, Ba, Ce



Magnetic dipole moment

$$\mu_{GS}(7/2^+, 7/2^-, 3/2^-)$$



- using the effective g factors the agreement with the data is far more satisfying than using the free g factors.
- a disagreement in $\mu(7/2^-)$ of ^{141}Ce remains unexplained.

Conclusions and Perspectives

- ✓ Our results achieved using N3LOP are in good agreement compared to the data.
 - ✓ First signs of the collectivity in the N=86,88 isotones was shown, with the signature of triaxial γ band.
 - ✓ Evolution of the collectivity is sensitive to SU(3) symmetries of neutrons and protons orbits sequence and to the excitations to $h_{11/2}$
 - ✓ These applications constitute a stringent test of N3LOP interaction, and our predictions are a benchmark for future experimental measurements.
- 👉 Extension of the calculations to higher mass number along isotopic and isotonic chains
- 👉 Explore the octupole correlations